

For each power series, find the radius of convergence and interval of convergence.

1.
$$\sum_{n=1}^{\infty} \frac{x^n}{\sqrt{n}}$$

2.
$$\sum_{n=0}^{\infty} (-1)^n \frac{n^2 x^n}{2^n}$$

3.
$$\sum_{n=0}^{\infty} \frac{x^n}{n!}$$

4.
$$\sum_{n=1}^{\infty} \sqrt{n} x^n$$

5.
$$\sum_{n=1}^{\infty} n! (2x - 1)^n$$

6.
$$\sum_{n=1}^{\infty} \frac{n(x - 4)^n}{n^3 + 1}$$

7.
$$\sum_{n=1}^{\infty} \frac{10^n x^n}{n^3}$$

8.
$$\sum_{n=1}^{\infty} \frac{n^2 x^n}{2 \cdot 4 \cdot 6 \cdots (2n)}$$